

2024

PHYSICS — HONOURS

Paper : DSE-A-2.1 and DSE-A-2.2

*The figures in the margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable.*

DSE-A-2.1

(Nanomaterials and Applications)

Full Marks : 65

Group - A

1. Answer *any five* questions :

2×5

- (a) Quantum dots are considered as artificial atoms. – Explain.
- (b) What do you mean by polaron?
- (c) An X-ray beam of wavelength 0.71\AA is diffracted by a cubic rock salt ($a = 0.281\text{ nm}$). Calculate the glancing angle for the second-order reflection from (110) planes.
- (d) Using Scherrer equation, calculate the crystallite size of nanoparticle with full width at half maximum (FWHM) = 0.1 radians, $\lambda = 0.154\text{ nm}$ and $\theta = 30^\circ$. (Scherrer constant = 0.9).
- (e) Show that the quantum size (Δx) effects become observable under the condition $\Delta x \leq \frac{\hbar}{\sqrt{mkT}}$.
(symbols have their usual meaning).
- (f) State the basic principle of NEMS.
- (g) Why is the sample covered by gold in SEM study?

Group - B

2. Answer *any three* questions :

- (a) (i) An electron is confined between two impenetrable walls 5\AA apart. Determine the energy levels for the states $n = 1$ and 3.
- (ii) Find the speed of the electron in the $n = 1$ state. 3+2
- (b) (i) What do you mean by density of states?
- (ii) Determine the density of states of a two-dimensional nanomaterial. Sketch the same as a function of energy. 1+(3+1)
- (c) (i) Briefly outline the spin coating and dip coating techniques using sol-gel method.
- (ii) Mention two advantages and two disadvantages of sol-gel method. 3+2

Please Turn Over

- (d) (i) What information can X-ray diffraction reveal about the structure of nanomaterials?
 (ii) Derive the Scherrer formula for determining the average particle size of nanocrystals. 2+3
- (e) (i) What are excitons?
 (ii) What are the different types of excitons? Distinguish between them. 2+(1+2)

Group - C

Answer *any four* questions.

3. (a) What is scanning electron microscopy (SEM)? Draw the schematic diagram and mention the essential components of a Scanning Electron Microscope.
 (b) What are the various signals produced by SEM regarding microstructure and chemical analysis of a nanomaterial?
 (c) How many atoms does a spherical gold nanoparticle of radius 1 nm contain given bulk gold has *fcc* structure with lattice constant 4.08 Å? (2+2)+2+4
4. (a) Chemical vapour deposition (CVD) is a bottom-up approach. – Explain.
 (b) What are the different types of CVD processes?
 (c) Describe the principle of operation of a CVD process.
 (d) What are the differences between chemical and physical vapour deposition techniques? 2+2+3+3
5. (a) What are the differences between Schottky and Frenkel defects?
 (b) Find an expression to show how the number of Schottky defects depend on temperature.
 (c) What are F centres? Explain with an example. 3+4+(2+1)
6. (a) What do you mean by magnetic quantum well? How does it differ from a traditional quantum well?
 (b) What are the major differences between conduction at the macroscale and nanoscale levels?
 (c) Distinguish between an exciton and a polaron. Explain why excitons do not contribute to electrical conduction. (2+2)+2+(2+2)
7. (a) Explain the Coulomb blockade effect. What conditions must be satisfied for this effect to be observed?
 (b) Show that a potential $\frac{e}{C}$ is required to transfer a single electron across a tunnel junction.
 (c) Calculate the size of a sphere-shaped quantum dot of Si that would produce observable single electron effect at room temperature (300 K).
 (The dielectric constant of silicon = 11.5, and the permittivity of vacuum, $\epsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$). (3+2)+2+3
8. (a) What do you mean by photoluminescence (PL)?
 (b) Mention briefly the use of nanostructured materials in solar cells, LEDs, optical data storage devices, and medical technology. 2+(2×4)

DSE-A-2.2**(Advanced Classical Dynamics)****Full Marks : 65****Group - A****1. Answer *any five* questions :****2×5**

- (a) A bob of mass ' m ' hangs from a rigid support with a massless inextensible chord and executes SHM. Use Lagrangian formulation to find the tension in the string.
- (b) If I_1 , I_2 and I_3 be the principal moments of inertia of a rigid body, then show that $I_3 \leq I_1 + I_2$.
- (c) Calculate the Poisson brackets $\{x, L_x\}$, where L_x is the x -component of the angular momentum of a particle.
- (d) For a particle having a Lagrangian $L = \dot{x}^2/(2x) - V(x)$, find the Hamiltonian H .
- (e) Show that for inverse square central force field, Virial theorem takes the form $2\langle T \rangle + \langle V \rangle = 0$, where the symbols have their usual meanings.
- (f) Find the fixed points for the dynamical system represented by $\dot{x} = \sin x$ and classify their stability.
- (g) What do you mean by dissipative dynamical system? Explain with one example.

Group - B**2. Answer *any three* questions :**

- (a) A particle is moving along a straight line under the action of a potential $V(x)$. Show that the Lagrange's equation of motion remains invariant under the transformation $x = c + x'$, where c is a constant. 5
- (b) Using Fermat's principle, find the path followed by light ray in a medium whose refractive index n is proportional to $1/y$. 5
- (c) State Virial theorem in classical mechanics. Derive the equation of state $PV = NK_B T$ for ideal gas from the concept of Virial theorem. 2+3
- (d) What are fixed points? Discuss the stability character of the fixed point for the system $\dot{x} = x(1-x)$ using the concept of flow. 2+3
- (e) Find the fixed points for the map $x_{n+1} = x_n^3$ and determine their stability. 5

Please Turn Over

Group - C

Answer **any four** questions.

3. (a) Given $S = \int_0^1 \frac{\dot{x}^2}{t^3} dt$. Extremize S to find $x(t)$ with conditions $x(t=0) = 1$ and $x(t=1) = 2$.

(b) If $f(q, p)$ and $g(q, p)$ are constants of motion, then show that their Poisson bracket $\{f, g\}$ is also a constant of motion.

(c) Using Poisson bracket, show that $F = \frac{pq}{2} - Ht$ is a constant of motion if the Hamiltonian of the

system is given by $H = \frac{p^2}{2m} - \frac{1}{2q^2}$. 4+3+3

4. (a) Consider a particle of mass m moving under the action of uniform gravity on the surface of a sphere of radius R . Show that the critical angle (θ_c) at which the particle sliding off from the surface of sphere is given by $\theta_c = \cos^{-1}(2/3)$. [Assume that the particle starts off from the North Pole]

(b) A particle of charge ' q ' and mass ' m ' moves with velocity $\vec{v}(t)$ in a region containing both electric field $\vec{E}(\vec{r}, t)$ and magnetic field $\vec{B}(\vec{r}, t)$. Show that the Lagrangian of the charged particle is given by

$$L = \frac{1}{2}mv^2 + q(\phi - \vec{A} \cdot \vec{v}),$$

where $\phi(\vec{r}, t)$ and $\vec{A}(\vec{r}, t)$ are electric scalar potential and magnetic vector potential, respectively.

5+5

5. (a) Show that the Poisson bracket of $\{L_x, L_y\} = L_z$, where L_x , L_y and L_z are the cartesian components of angular momentum.

(b) For a system, kinetic energy $T = \frac{1}{2}m\dot{r}^2$ and potential energy $V = \frac{1}{r} \left(1 + \frac{\dot{r}^2}{c^2} \right)$.

(i) Find the Hamiltonian (H) of the system.

(ii) Determine whether $H = T + V$.

(iii) Show that $\frac{dH}{dt} = 0$.

- (c) Show that if the Lagrangian of a system does not depend on time explicitly, its Hamiltonian is a constant of motion. 3+3+4

6. (a) Consider a linear triatomic molecule with two outer atoms of mass m connected to central atom of mass M by two identical massless springs of spring constant s . Show that the normal frequencies of small oscillation are

$$0, \sqrt{s/m}, \sqrt{(s/m) + (2s/M)}.$$

- (b) Find the moments and products of inertia of a uniform square plate of side ' a ' and mass ' m ' about x, y, z axes, x, y being taken as the adjacent sides of the plate and z is perpendicular to its plane. Also calculate the principal moments of inertia. 5+(3+2)
7. (a) What do you mean by a 'dynamical system'? Cast the equation of Newton's laws of motion for a particle moving along x -axis, $m\ddot{x} = f(x)$, into a dynamical system. What is its dimensionality?
- (b) Find the fixed points of the dynamical system represented by $\dot{x} = x^2 - 1$. Draw the phase portrait and the flow of x . Hence, ascertain the nature of the fixed points. (2+1+1)+(2+2+2)
8. (a) Consider two models for the population growth (i) $\dot{N} = rN$, and (ii) $\dot{N} = rN \left(1 - \frac{N}{k}\right)$.

Find the fixed point(s) in each case. Use the linear stability analysis to study the nature of the fixed points.

- (b) Consider the map $x_{n+1} = \cos x_n$. Using the quadratic MacLaurin expansion for the cosine function, find the approximate values for the fixed point(s) of the system. How many fixed point does the system has? (1+2+3)+(3+1)